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Introduction to Medical Image Processing (5XSA0), Module 03

Image Restoration and Freq. Filtering & Color Imaging and Transformations

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slides version 1.0

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Overview Module 03

- * **Part 1a: Noise and filtering**
 - Noise models, Spatial filtering and periodic noise
- * **Part 1b: Special filtering techniques**
 - Frequency-Band Filtering,
 - Adaptive filtering
- * **Part 2: Color imaging and transformations**
 - Color models and systems
 - Color representations and associated processing
- * **Part 3: Cases with medical image restoration**
 - Case 1: Ultrasound imaging, Case 2: Cancer detection, analysis

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Module 03 – Part 1 Image Restoration & Reconstruction

Noise models, spatial noise filters, freq.-domain noise filters, projection imaging and CT

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Model of Image Degradation/Restoration

1. Model communication imperfections and noise insertion by a channel with degradation and restoration filters.
2. Degradation can be derived by measuring and analysis
3. Model is linear (pos. invariant) 'filter' process & addition of noise, so

$$g(x, y) = h(x, y) \otimes f(x, y) + n(x, y)$$

$$G(u, v) = H(u, v)F(u, v) + N(u, v)$$

FIGURE 5.1 A model of the image degradation/restoration process.

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Noise Sources and Considerations

1. Noise is generated when capturing the image, caused by
 1. **Sensor: intrinsic noise and temperature**
 2. **Light level of the scene**
 3. **Insufficient resolution processing (cost reduction)**
2. Noise has spatial and frequency properties, so it can be analyzed with the DFT and in time domain
3. For analysis purposes (also here), noise is assumed to be spatially and signal independent. This is sometimes invalid (e.g. X-ray and nuclear medicine imaging)

$$g(x, y) = h(x, y) \otimes f(x, y) + n(x, y)$$

$$G(u, v) = H(u, v)F(u, v) + N(u, v)$$

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Widely Used Noise Models – (1)

1. **Gaussian (normal) noise**

$$p(z) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(z-\mu)^2}{2\sigma^2}}$$
 1. Mathematically tractable
 2. Note mean μ and st.dev. σ
2. **Rayleigh noise**

$$p(z) = \frac{2}{b} (z-a) e^{-\frac{(z-a)^2}{b}} \quad (z \geq a)$$
 1. Often in comm. problems
 2. Has mean and variance with

$$\bar{z} = \mu = a + \sqrt{\pi b}/4; \quad \sigma^2 = b(4-\pi)/4$$
3. **Erlang (Gamma) noise**

$$p(z) = \frac{a^b z^{b-1}}{(b-1)!} e^{-az} \quad (z \geq 0)$$
 1. Has mean and variance
 2. $a > 0$ and b positive integer

$$\bar{z} = \mu = b/a; \quad \sigma^2 = b/a^2$$

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Widely Used Noise Models – (2) 7

1. **Exponential noise**

$$p(z) = ae^{-az} \quad (a, z \geq 0)$$
 1. Mathematically tractable
 2. Note mean μ and st.dev. σ

$$\mu = 1/a; \quad \sigma^2 = 1/a^2$$
2. **Uniform noise**

$$p(z) = \frac{1}{b-a}; \quad (a \leq z \leq b)$$
 1. Often in analysis problems
 2. Has mean and variance with

$$\mu = (a+b)/2; \quad \sigma^2 = (b-a)^2/12$$
3. **Impulse (salt and pepper) noise**

$$p(z) = P_a \quad (z = a)$$

$$p(z) = P_b \quad (z = b)$$
 1. Noise pulses can be pos. or negative
 2. $b > a$, intensity b will be light dot
 3. If either probability is zero: unipolar noise

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Illustrated noise models 8

FIGURE 5.2 Some important probability density functions.

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Adding noise models to images – (1) 9

FIGURE 5.4 Images and histograms resulting from adding Gaussian, Rayleigh, and gamma noise to the image in Fig. 5.3.

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Adding noise models to images – (2) 10

FIGURE 5.4 (Continued) Images and histograms resulting from adding exponential, uniform, and salt and pepper noise to the image in Fig. 5.3.

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Periodic noise 11

- Periodic noise is spatially dependent (exception!)
- Very suited for filtering in the frequency domain!
- Model is sinusoid, with

$$r(x, y) = A \sin[2\pi u_0(x + B_x) / M + 2\pi v_0(y + B_y) / N]$$
- u and v are frequencies, B 's are phase (displacements)
- Derive the frequency domain representation

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Periodic noise – Visual example 12

- Periodic noise is spatially dependent

FIGURE 5.5 (a) Image corrupted by sinusoidal noise. (b) Spectrum (each pair of conjugate impulses corresponds to one sine wave). (Original image courtesy of NASA.)

Note spectrum dots!
Each sine wave gives a conjugate pair in freq. domain

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Measuring noise parameters

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- Take selected area(s) of image which have no detail and measure the local histogram
- Measure e.g. mean and variance

$$\mu = \sum_{z=0}^{L-1} z_i p_s(z_i)$$

$$\sigma^2 = \sum_{z=0}^{L-1} (z - \mu)^2 p_s(z_i)$$

FIGURE 5.6 Histograms computed using small strips (shown as inserts) from (a) the Gaussian, (b) the Rayleigh, and (c) the uniform noisy images in Fig. 5.4.

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Spatial mean filtering / restoration of noise

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Covers the case of noise only $g(x, y) = f(x, y) + n(x, y)$

- Arithmetic mean filter**
 - Simple filter, average in area
 - Rectangular window $m \times n$
$$\hat{f}(x, y) = \frac{1}{mn} \sum_{(s,t) \in S_{xy}} g(s, t)$$
- Geometric mean filter**
 - Perform similar to mean filter
 - Tends to lose less details
$$\hat{f}(x, y) = \left[\prod_{(s,t) \in S_{xy}} g(s, t) \right]^{\frac{1}{mn}}$$
- Harmonic mean filter**
 - Works well for salt noise, not pepper
 - Performs well also for Gaussian noise
$$\hat{f}(x, y) = \frac{mn}{\sum_{(s,t) \in S_{xy}} \frac{1}{g(s, t)}}$$

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Mean filtering – Example X-ray image – 1

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FIGURE 5.7 (a) X-ray image. (b) Image corrupted by additive Gaussian noise. (c) Result of filtering with an arithmetic mean filter of size 3×3 . (d) Result of filtering with a geometric mean filter of the same size. (Original image courtesy of Mr. Joseph E. Pascentie, Lixi, Inc.)

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Mean filtering – Example of X-ray image – 2

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FIGURE 5.8 (a) Image corrupted by pepper noise with a probability of 0.1. (b) Image corrupted by salt noise with the same probability. (c) Result of filtering (a) with a 3×3 contraharmonic filter of order 1.5. (d) Result of filtering (b) with $Q = -1.5$.

$$\hat{f}(x, y) = \frac{\sum_{(s,t) \in S_{xy}} g(s, t)^{Q+1}}{\sum_{(s,t) \in S_{xy}} g(s, t)^Q}$$

Contraharmonic mean filter reduces salt-&-pepper noise

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Mean filtering – Example of X-ray image – 3

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FIGURE 5.9 Results of selecting the wrong sign in contraharmonic filtering. (a) Result of filtering Fig. 5.8(a) with a contraharmonic filter of size 3×3 and $Q = -1.5$. (b) Result of filtering 5.8(b) with $Q = 1.5$.

In general, arithmetic or geometric mean filters are well suited for random noise (such as Gaussian, uniform). The contraharmonic filter does well for impulse noise, but the dark/light color has to be known.

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Order-statistic filters / Median etc.

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Covers the case of noise only. Order-statistic filters are spatial filters whose response is based on **ordering/ranking the pixels. Is a non-linear process.**

- Median filter**
 - Widely applied
 - Selects the median of a set of samples
 - Excellent results for speckle noise, no blur
$$\hat{f}(x, y) = \text{median} \{g(s, t)\}_{(s,t) \in S_{xy}}$$
- Max and min filter**
 - Useful for finding bright/dark points
 - Max filter reduced pepper noise
 - Min filter reduced salt noise
$$\hat{f}(x, y) = \max \{g(s, t)\}_{(s,t) \in S_{xy}}$$

$$\hat{f}(x, y) = \min \{g(s, t)\}_{(s,t) \in S_{xy}}$$

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Example results with 3x3 Median filters

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FIGURE 5.10
 (a) Image corrupted by salt-and-pepper noise with probabilities $P_s = P_p = 0.1$.
 (b) Result of one pass with a median filter of size 3×3 .
 (c) Result of processing (b) with this filter.
 (d) Result of processing (c) with the same filter.

Median, one iter.

Median, three iter.

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Example results with max/min filters

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FIGURE 5.11
 (a) Result of filtering Fig. 5.8(a) with a max filter of size 3×3 . (b) Result of filtering 5.8(b) with a min filter of the same size.

Note the brightening effect of the max filter and the darkening effect of the min filter!

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Sample results with mean & median filters

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FIGURE 5.12
 (a) Image corrupted by additive uniform noise.
 (b) Image additionally corrupted by additive salt-and-pepper noise. Image (b) filtered with a 5×5 ; (c) arithmetic mean filter; (d) geometric mean filter; (e) median filter; and (f) alpha-trimmed mean filter with $d = 5$.

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Adaptive filters

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Adaptive filters

- * Perform better than static filters as presented earlier
- * They have a higher complexity, since measurements are required
- * Operate within a window and then adapt to the image contents

1. Adaptive local noise reduction filter, operating in area S , depending on 4 quantities

1. $g(x, y)$ the value of the noisy image
2. σ_{η}^2 , the variance of the noise corrupting $f(x, y)$
3. the local mean m_L of the pixels in the window
4. σ_L^2 , the local variance of the pixels in the window

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Local noise reduction filter

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* **The desired behavior of the filter should be that**

1. If $\sigma_{\eta}^2 = 0$ the filter should return simply the value of $g(x, y)$
2. If the local variance is high relative to σ_{η}^2 , the filter should return a value close to $g(x, y)$. Edges should be preserved.
3. If the two variances are equal, the filter should return the arithmetic mean value of the pixels in S . This means that the local area has the same properties as the overall image and local noise then averaged.

The filter could be as follows

$$\hat{f}(x, y) = g(x, y) - \frac{\sigma_{\eta}^2}{\sigma_L^2} [g(x, y) - m_L]$$

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Local noise reduction filter - Result

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FIGURE 5.13
 (a) Image corrupted by additive Gaussian noise of zero mean and variance 1000. (b) Result of arithmetic mean filtering. (c) Result of geometric mean filtering. (d) Result of adaptive noise reduction filtering. All filters were of size 7×7 .

Adaptive filters are always better!

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Adaptive median filter – (1)

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- Normal median filter can handle low-density noise
- Varying density noise requires other filtering
- An adaptive median filter may change the filter window S
- The filter still replaces one pixel with the filter output
- Consider that z_{\min} = min of window, z_{\max} = max of window, z_{med} = median of window, S_{\max} = max window size

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Adaptive median filter – (2) / Algorithm

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Stage A

- $A1 = z_{\text{med}} - z_{\min}$; $A2 = z_{\text{med}} - z_{\max}$.
- If $A1 > 0$ and $A2 < 0$, go to stage B
- Else increase window size
- If window size $\leq S_{\max}$ repeat stage A
- Else output z_{med}

Determine in this stage, whether output z_{med} is impulse or not

Stage B

- $B1 = z_{xy} - z_{\min}$; $B2 = z_{xy} - z_{\max}$.
- If $B1 > 0$ and $B2 < 0$, output z_{xy}
- Else output z_{med}

Test whether data is impulse or not, if so, then filter

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Adaptive median filter – (3) / Results

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FIGURE 5.14 (a) Image corrupted by salt-and-pepper noise with probabilities $P_s = P_p = 0.25$. (b) Result of filtering with a 7×7 median filter. (c) Result of adaptive median filtering with $S_{\max} = 7$.

Static filter shows a significant loss of detail (broken conn.)!

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Frequency domain filters – Bandreject

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Sometimes, the spectral noise location is known, e.g. with periodic noise. Then define specific spectral noise filters

FIGURE 5.15 From left to right, perspective plots of ideal, Butterworth (of order 1), and Gaussian bandreject filters.

Additive periodic noise can be approximated by 2-d sinusoidal functions. Remember the DFT of sine is two conjugate impulses!

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Frequency domain filters – Bandreject

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FIGURE 5.16 (a) Image corrupted by sinusoidal noise. (b) Spectrum of (a). (c) Butterworth bandreject filter (white represents 1). (d) Result of filtering. (Original image courtesy of NASA.)

Bandpass filter is opposite of bandreject, hence

$$H_{BP} = 1 - H_{BR}$$

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Frequency domain filters – Bandpass

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Bandpass filter is opposite of bandreject, hence

$$H_{BP}(u,v) = 1 - H_{BR}(u,v)$$

FIGURE 5.17 Noise pattern of the image in Fig. 5.16(a) obtained by bandpass filtering.

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Frequency domain filters – Notch filters

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FIGURE 5.18
Perspective plots of (a) ideal, (b) Butterworth (of order 2), and (c) Gaussian notch (reject) filters.

A notch filter rejects (passes) frequencies in a neighborhood about a center

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Freq.-domain filters – Notch filter results

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FIGURE 5.19
(a) Satellite image of Florida and the Gulf of Mexico showing horizontal scan lines. (b) Spectrum. (c) Notch pass filter superimposed on (b). (d) Spatial response pattern. (e) Result of notch reject filtering. (Original image courtesy of NOAA.)

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Estimation of the degradation function

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Obtain the degradation by

- * **Observation**
 - Function is not known
 - Measure in rectangles in foreground and background
- * **Experimentation**
 - Perform experiments with equipment to emulate conditions
 - Impose image impulse, measure impulse response, $H=G(u, v)/A$
- * **Mathematical modeling**
 - Test with modeled filters, such as Gaussian, Laplacian etc.

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Example: blur caused by linear motion - 1

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- * Consider the shift $g(x, y) = \int_0^T f[x - x_0(t), y - y_0(t)] dt$
- * Integration constant with time T and g the blurred image
- * Taking the Fourier transform and reversing the integration over T with that of Fourier gives

$$G(u, v) = \int_0^T F(u, v) e^{-j2\pi[u x_0(t) + v y_0(t)]} dt = F(u, v) H(u, v)$$

- * Hence, H is the integral over de exponential
- * If the motion variables, are known, then H is computed

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Example: blur caused by linear motion - 2

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- * Consider the function $x_0(t) = at/T$
- * Taking the Fourier transform and deriving further

$$H(u, v) = \int_0^T e^{-j2\pi u x_0(t)} dt = \int_0^T e^{-j2\pi u at/T} dt = \frac{T}{\pi u a} \sin(\pi u a) e^{-j\pi u a}$$

- * This result can be extended in 2D with $y_0(t) = bt/T$

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Example: blur caused by linear motion - 3

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FIGURE 5.26
(a) Original image. (b) Result of blurring using the function in Eq. (5.6-11) with $a = b = 0.1$ and $T = 1$.

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Inverse filtering

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Suppose we have degradation function $H(u,v)$

* **Simplest approach: inverse filtering**

- $F^h(u,v) = G(u,v) / H(u,v)$, then with add. noise, we find
- $F^h(u,v) = F(u,v) + N(u,v) / H(u,v)$
- Note that $N(u,v)$ is not known!
- Also: when $H(u,v)$ is zero, then the ratio explodes...., this happens frequently
- One way around: limit filter frequencies to values close to origin where H is high typically

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Module 03 – Part 2 Color image processing

Color fundamentals, triangle, color models, color conversion

Color processing

- * **Full-color processing**
 - Involves TV, broadcast and consumer cameras, etc
- * **Pseudo color processing**
 - Often used in medical domain: generate color to show...

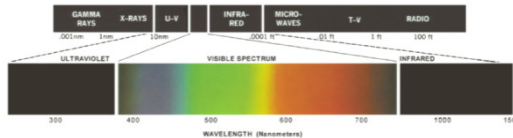


FIGURE 6.2 Wavelengths comprising the visible range of the electromagnetic spectrum. (Courtesy of the General Electric Co., Lamp Business Division.)

Color light wavelengths

- * **Human eye cones measure light**
 - 65% red, 33% green, 2% blue
 - All cones not equal!
- * **RGB are thus primary colors**
 - Blue=435nm
 - Green= 546nm
 - Red=700nm

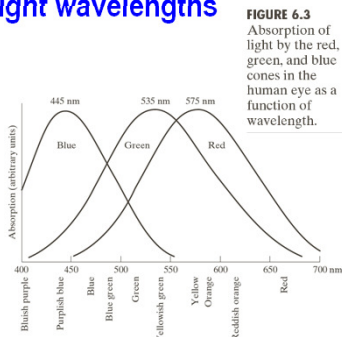


FIGURE 6.3 Absorption of light by the red, green, and blue cones in the human eye as a function of wavelength.

Color mixtures

- * **Primary colors can be mixed to secondary colors**
 - Magenta=R+B
 - Cyan=G+B
 - Yellow=R+G
- * **Mixing secondary color with an opposite primary (or 3 prim.) gives white**

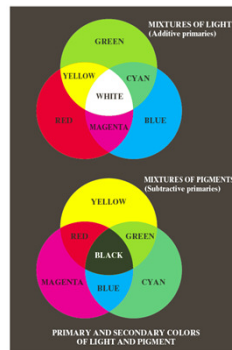


FIGURE 6.4 Primary and secondary colors of light and pigments. (Courtesy of the General Electric Co., Lamp Business Division.)

Color triangle

- * **Colors have been specified by CIE**
 - In a triangle
 - x (red) and y (green)
 - z (blue) = $1 - (x+y)$
- * **Any point on boundary is fully saturated**

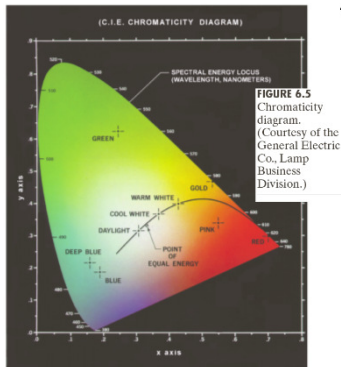


FIGURE 6.5 Chromaticity diagram. (Courtesy of the General Electric Co., Lamp Business Division.)

Typical color models

- * **Color is specified in models**
 - RGB, Red Green Blue, for TV & cameras
 - CMYK, Cyan Magenta Yellow Black, for printing
 - The color black in CMYK is extra
 - HSI, Hue Saturation Intensity, for grayscale printing, old TV, etc

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RGB Color Model

- * RGB is based on Cartesian coordinates, RGB on axes, CMY on corners, Black at origin

FIGURE 6.7 Schematic of the RGB color cube. Points along the main diagonal have gray values, from black at the origin to white at point (1, 1, 1).

FIGURE 6.8 RGB 24-bit color cube. 16M colors!

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RGB safe color cube for coloring images

- * RGB safe color cube: only colors at the surface of the cube, total 216 colors
- * Guarantee colors at every 8-bit computer/display
 - Each surface has 6x6 colors
 - All 8-bit gray levels are included
 - supports web-based & pseudo-color imaging

FIGURE 6.11 The RGB safe-color cube.

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CMY and CMYK Color Models

- * CMY are secondary colors, or **primary colors of pigments**
- * Printing popularity comes from: cyan does not reflect red from white light illumination
- * Most devices using colored pigments require CMY input
- * Conversion from RGB is simple, and results from $(C, M, Y)^T = (I, I, I)^T - (R, G, B)^T$
- * Based on assumption that all colors have been normalized to unit interval
- * Note that first component equation reflects absence of red, magenta reflects no green, and yellow no blue.
- * Likewise, RGB can be easily obtained from CMY

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HSI Color Model

- * HSI originates from the wish to describe images in
 - Intensity (black & white or gray level image)
 - Saturation (strength of the pure color component)
 - Hue (color temperature, simply the type of color)
- * HSI is much more suited for describing color images, rather than RGB, that is more suited for color image generation
- * Convert from RGB cube, by tilting it such that black is at the bottom and white at the top....

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HSI Color understanding the RGB cube

- * Convert from RGB cube, by tilting it such that black is at the bottom and white at the top....
- * Intensity is covered by passing a plane perpendicular to the intensity axis, and hue is in the shaded plane

FIGURE 6.12 Conceptual relationships between the RGB and HSI color models.

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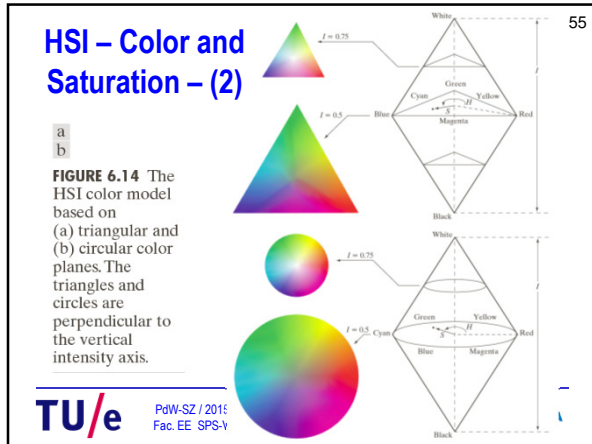
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HSI – Color and Saturation – (1)

- * Convert from RGB cube, cross planes are triangular or hexagonal
- * Hue is angle leftwise from red orientation
- * Saturation is the length of the vector
- * Origin is at intersection with intensity plane

FIGURE 6.13 Hue and saturation in the HSI color model. The dot is an arbitrary color point. The angle from the red axis gives the hue, and the length of the vector is the saturation. The intensity of all colors in any of these planes is given by the position of the plane on the vertical intensity axis.

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Converting color from RGB to HSI – (1)

- * From each RGB pixel, the H value $H = \theta \quad B \leq G$
 $H = 360 - \theta \quad B > G$
- * The angle comes from a.o. goniometry analysis
$$\theta = \arccos\left\{\frac{1/2[(R-G)+R-B]}{[(R-G)^2 + (R-B)(G-B)]^{1/2}}\right\}$$
- * The saturation and intensity are given by
$$S = 1 - \frac{3}{(R+G+B)}[\min(R, G, B)] \quad I = \frac{1}{3}(R+G+B)$$

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Converting color from RGB to HSI – (2)

Note the following properties

- RGB colors in (a) have fixed saturation
- Intensity grows when more color is added

FIGURE 6.16 (a) RGB image and the components of its corresponding HSI image: (b) hue, (c) saturation, and (d) intensity.

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Pseudo color - Intensity slicing

- Let the gray scale vary between 0 (black) and $L-1$ (white)
- Assume P planes perpendicular to the intensity axis
- $P+1$ partitions of gray scale are made
- Each value intensity I_k converts to color c_k

FIGURE 6.17 (a)-(c) Modified HSI component images, (d) Resulting RGB image. (See Fig. 6.16 for the original HSI images.)

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Geometric interpretation of intensity slicing

FIGURE 6.18 Geometric interpretation of the intensity-slicing technique.

FIGURE 6.19 An alternative representation of the intensity-slicing technique.

$f(x, y) = c_k \quad \text{if} \quad f(x, y) \in V_k$

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Color / Example of intensity slicing

FIGURE 6.20 (a) Monochrome image of the Picker Thyroid Phantom, (b) Result of density slicing into eight colors. (Courtesy of Dr. J. L. Blankenship, Instrumentation and Controls Division, Oak Ridge National Laboratory.)

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Module 03 – Part 3 Medical Cases with Image Restoration and Frequency

Case 1: UltraSound imaging of needles &

Contributed by ir. Arash Poutaherian

Case 2: Frequency analysis of colon cancer

Contributed by ir. Fons van der Sommen



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Case 1: Ultrasound-guided interventions

* Ultrasound-guided interventions with needles



Contributed
by ir. Arash
Poutaherian



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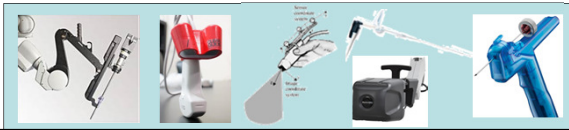
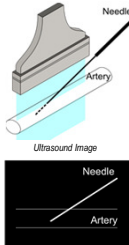
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Case 1 / Example 2 US - Challenges

* Limited field of view in 2D ultrasound:

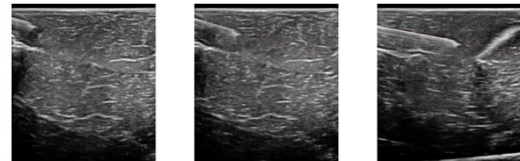
- Any motion may exclude parts of the needle from ultrasound field.
- Considerable training is required to avoid wrong needle placement.
- Extremely challenging, tense, lengthy procedure.

* Existing tracking systems (electromagn., optical, robotics) require extra equipment, specific skills, add to the costs.



Case 1: Ultrasound Image Proc. Challenges

- * Low signal to noise, e.g. spurious speckle noise occurs
- * Various imaging artifacts (e.g. ringing, limited depth)
- * Needle visibility decreases with the insertion angle
- * During an intervention, only short parts of the needle are visible in initial frames



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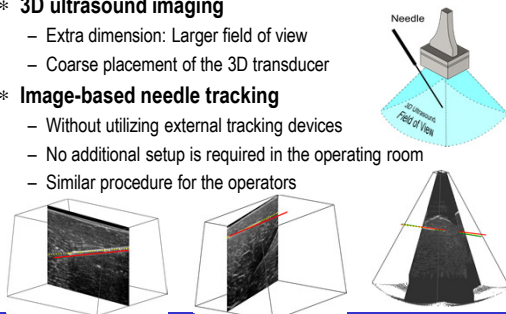
Case 1: Ultrasound Proposed System

* 3D ultrasound imaging

- Extra dimension: Larger field of view
- Coarse placement of the 3D transducer

* Image-based needle tracking

- Without utilizing external tracking devices
- No additional setup is required in the operating room
- Similar procedure for the operators

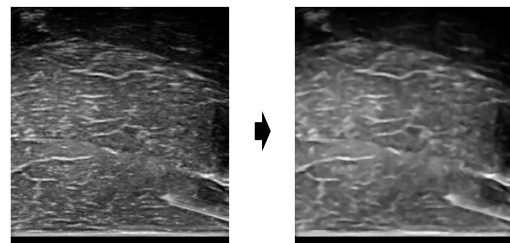


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Case 1: Ultrasound image restoration – (1)

- * Assuming the speckle noise as an *impulsive* effect, **median filtering** can be used to reduce the speckles.

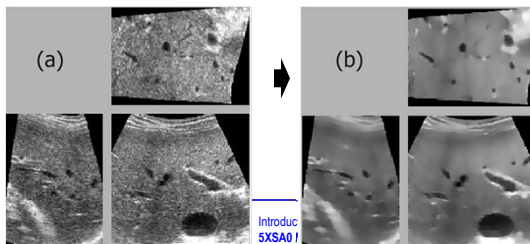


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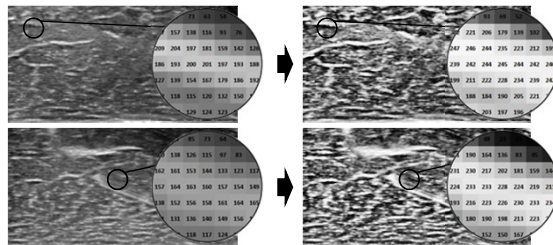
Case 1: Ultrasound image restoration – (2) ⁶⁷

- * Anisotropic-diffusion filters reduce speckles by smoothing noisy regions with a Gaussian filter.
- * The rate of diffusion is controlled by local statistics such as the image gradient.



Case 1: Ultrasound image restoration – (3) ⁶⁸

- * Adaptive histogram equalization minimizes the difference in needle brightness at different insertion angles.



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Case 2: Esophageal cancer detection with visual imaging ⁶⁹

- Risk factors: obesity, reflux, genetics



This case is contributed by ir. Fons van der Sommen

- Fastest rising type of cancer in the Western world
- 5th most prevalent cancer, 10-15% five-year survival rate
- 80% of patients are diagnosed in a late stadium
 - Esophagectomy – up to 10% die due to surgery complications
 - High morbidity – trouble with eating etc.

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Case 2: Detection esophageal cancer – “dream” ⁷⁰



- * Supportive detection system for the detection of early esophageal cancer.
- * Early detection: 100% five-year-survival-rate* instead of 10-15% for esophageal cancer.

* Patients who have died due to other implications are not included.

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Case 2: Esophageal cancer / Objective ⁷¹

Create a real-time computer aided detection system which aids the physician to identify early cancer in the esophagus

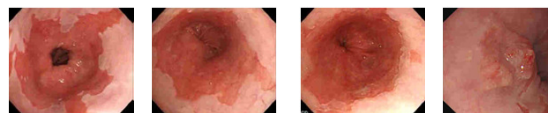
Applications

Real-time detection:
• endoscopy examination and surgery

Off-line detection:
• training gastroenterologists
• quality assurance in existing databases

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Case 2: Esophagus cancer evolves gradually ⁷²



Advanced stage cancer

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Case 2: Detection cancer – special direct. filters ⁷³

- * Use **specially tuned filters** to quantize deviating texture related to early lesions.
- * Employ **machine learning techniques** to differentiate between cancerous and non-cancerous tissue.

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Case 2: Detection cancer – Experiment. results ⁷⁴

- * **Latest study with 5 international experts**
- * Detection performance close to expert level.
- * Precision/recall:
System: 0.71/0.88 to 1.00/0.70
Experts: 0.85/0.81 to 1.00/0.72

Patient-based detection of early cancer					
	Early carcinoma	High-grade dysplasia	False detection		
System ps1	9 / 13	6 / 8	2		
System ps2	12 / 13	6 / 8	2		
System ps3	13 / 13	5 / 8	0		
Expert 2	13 / 13	6 / 8	2		
Expert 3	13 / 13	5 / 8	4		
Expert 4	13 / 13	7 / 8	0		
Expert 5	13 / 13	7 / 8	4		

System Expert 1 (Gold standard) Expert 2 Expert 3 Expert 4 Expert 5

Case 2: Frequency analysis – (1) ⁷⁵

Example: detection of cancerous tissue

- * Known from medical literature: difference in texture.
- * Texture can be considered as a **combination of frequencies**.
– We can analyze frequencies using the Fourier transform!
- * Question: Can we observe the difference between cancerous tissue and healthy tissue in the **frequency domain**?
- * If we can, we can develop filters for these frequencies to **discriminate** between cancer and healthy tissue.

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Case 2: Frequency analysis – (2) ⁷⁶

Image annotated by medical expert Split the image in 50 × 50

Analyze spectrum for the cancer blocks (red) and the healthy blocks (green). Exclude ambiguous blocks from analysis (yellow).

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Case 2: Frequency analysis – (3) ⁷⁷

Can we find the exact frequencies?

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Case 2: Frequency analysis – (4) ⁷⁸

- * We are not interested in the orientation, so let us integrate θ out: $F(\omega) = \int F(\omega, \theta) d\theta$

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